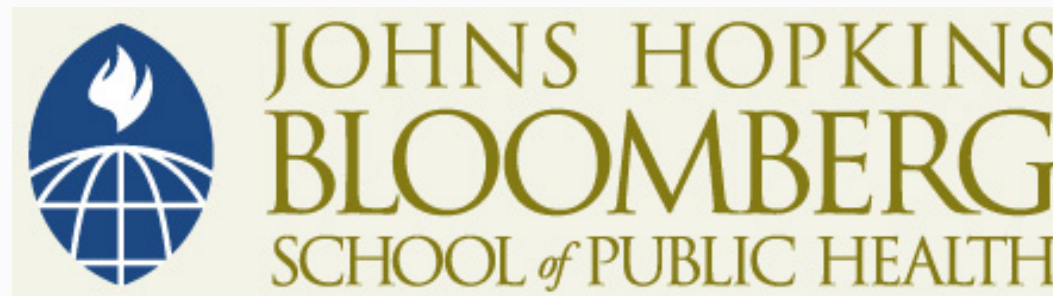


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Section F (Optional)

Non-Parametric Analogue to the Two Sample t-test

Alternative to the Two Sample T-Test

- Nonparametric test for comparing two groups
- “Non-parametric” refers to a class of tests that do not assume anything about distribution of the data
- Nonparametric test for comparing two groups
 - Mann-Whitney Rank Sum Test (Wilcoxon Rank Sum Test)
 - Also called Mann-Whitney-Wilcoxon (a mouthful)
- Tries to answer the following question:
 - Are the two population distributions different?

Advantages

- Does not assume populations being compared are normally distributed
 - The two-sample t-test requires that assumption with very small samples sizes
- Uses only ranks
- Not sensitive to outliers

Disadvantage of the Nonparametric Test

- Nonparametric methods are often less sensitive (powerful) for finding true differences because they throw away information (they use only ranks)
- Need full data set, not just summary statistics
- Results do not include any confidence intervals quantifying range of possibility for true difference between populations

Example: Health Education Study

- Evaluate an intervention to educate high school students about health and lifestyle over a two-month period
- 10 students randomized to “intervention” or “control” group
- $x = \text{post test score} - \text{pre-test score}$ is outcome to compare between the intervention and control groups

Example: Health Education Study

- x = post- pretest score for both groups
- Intervention (I) 5 0 7 2 19
- Control (C) 6 -5 -6 1 4
 - Only five individuals in each sample!!!
 - We want to compare the control and intervention groups to assess whether the “improvement” (post-pre) in scores are different, taking random sampling error into account

Example: Health Education Study

- With such a small sample size, we need to be sure score improvements are normally distributed if we want to use t-test (BIG assumption)
- Possible approach:
 - Mann-Whitney-Wilcoxon non-parametric test!

Example: Health Education Study

- First step—rank the pooled data (ignore groupings)

	-6	-5	0	1	2	4	5	5	7	19
— Rank	1	2	3	4	5	6	7	8	9	10

Example: Health Education Study

- Second step—“reattach” group status

	-6	-5	0	1	2	4	5	5	7	19
— Rank	1	2	3	4	5	6	7	8	9	10
— Group	C	C	I	C	I	C	I	C	I	I

Example: Health Education Study

- Find the average rank in each of the two groups
- Intervention group average rank

$$\frac{3 + 5 + 6 + 9 + 10}{5} = 6.8$$

- Control group average rank

$$\frac{1 + 2 + 4 + 6 + 8}{5} = 4.2$$

Example: Health Education Study

- Statisticians have developed formulas and tables to determine the probability of observing such an extreme discrepancy in ranks (6.8 vs. 4.2) by chance alone
 - This is the p-value
- In the health education study, the p-value was .17
 - The interpretation is that the Mann-Whitney test did not show any significant difference in test score “improvement” between the intervention and control group ($p = .17$)

Notes

- The two-sample t-test would give a different answer ($p = .14$)
- Different statistical procedures can give different p-values
- If the largest observation, 19, was changed, the p-value based on the Mann-Whitney test would not change but the two-sample t-test would change

Notes

- The t-test or the nonparametric test?
 - Statisticians will not always agree, but there are some guidelines
 - Use non-parametric test if sample size is small and you have no reason to believe data is “well behaved” (normally distributed)
 - Only “ranks” available

Using Stata to Perform Mann-Whitney-Wilcoxon

- Data, as entered

```
. list diff int_cntrl
```

```
+-----+
| diff   int_cntrl |
+-----+
1. |     4           0 |
2. |     1           0 |
3. |    -6           0 |
4. |    -5           0 |
5. |     6           0 |
+-----+
6. |    19           1 |
7. |     2           1 |
8. |     7           1 |
9. |     0           1 |
10. |     5           1 |
+-----+
```

Using Stata to Perform Mann-Whitney-Wilcoxon

- “ranksum” command

- Syntax:

- ▶ `ranksum varname, by(group_var)`

```
. ranksum diff, by( int_cntrl)
```

```
Two-sample Wilcoxon rank-sum (Mann-Whitney) test
```

int_cntrl	obs	rank sum	expected
0	5	21	27.5
1	5	34	27.5
combined	10	55	55

```
unadjusted variance      22.92
```

```
adjustment for ties      0.00
```

```
adjusted variance      22.92
```

```
Ho: diff(int_cntrl==0) = diff(int_cntrl==1)
```

```
z = -1.358
```

```
Prob > |z| = 0.1745
```


Using Stata to Perform Mann-Whitney-Wilcoxon

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 - ▶ `ranksum varname, by(group_var)`

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```
Ho: diff(int_cntrl==0) = diff(int_cntrl==1)
```

```
z = -1.358
```

```
Prob > |z| = 0.1745
```

Using Stata to Perform t-test

- “*ttest*” command without “*i*” on end when data already in Stata

- Syntax:

- ▶ *ttest varname, by(group_var)*

```
. ttest diff, by( int_cntrl)
```

```
Two-sample t test with equal variances
```

Group	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
0	5	0	2.387467	5.338539	-6.628672	6.628672
1	5	6.6	3.325658	7.436397	-2.633506	15.83351
combined	10	3.3	2.221361	7.02456	-1.725068	8.325068
diff		-6.6	4.093898		-16.04055	2.840545

```
diff = mean(0) - mean(1)
```

```
t = -1.6122
```

```
Ho: diff = 0
```

```
degrees of freedom = 8
```

```
Ha: diff < 0  
Pr(T < t) = 0.0728
```

```
Ha: diff != 0  
Pr(|T| > |t|) = 0.1456
```

```
Ha: diff > 0  
Pr(T > t) = 0.9272
```

Summary: Educational Intervention Example

■ **Statistical methods**

- 10 high school students were randomized to either receive a two-month health and lifestyle education program (or no program)
- Each student was administered a test regarding health and lifestyle issues prior to randomization (and after the two-month period)

Summary: Educational Intervention Example

■ **Statistical methods**

- Differences in the two test scores (after-before) were computed for each student
- Mean and median test score changes were computed for each of the two study groups
- A Mann-Whitney rank sum test was used to determine if there was a statistically significant difference in test score change between the intervention and control groups at the end of the two-month study period

Summary: Educational Intervention Example

■ Result

- Participants randomized to the educational intervention scored a median five points higher on the test given at the end of the two-month study period, as compared to the test administered prior to the intervention
- Participants randomized to receive no educational intervention scored a median one point higher on the test given at the end of the two-month study period
- The difference in test score improvements between the intervention and control groups was not statistically significant ($p = .17$)